adsorbed by the exterior surfaces of SWNTs and/or the interstitial spaces between bundled tubes. A vehicle powered by a fuel cell would require ~3.1 kg of H₂ for a 500 km range[17]. This amount of H₂ stored in the weight and volume of a typical petrol tank requires system densities approaching 6.5 wt% and 62 kg H₂ m⁻³ (ref. 17). Figure 2 shows that no storage technology is currently capable of meeting these goals. SWNTs with diameters of 16.3 Å and 20 Å would come close to the target densities and operate near room temperatures if modest H₂ overpressures compensated for the lower heats of adsorption expected in the larger cavities. These materials would have high energy storage efficiencies as they would operate at or near ambient temperatures and pressures. In contrast, 25 to 45% of the energy content in liquefied H₂ is required for liquefaction, and ~99% of the stored energy is needed for compression of H₂ to 20 MPa (ref. 17). For catalytic generation of H₂ by the reaction of H₂O with iron, temperatures in excess of 250°C are required[17,18].

The effect of hydrogen over-pressure on the stability of adsorbed H₂ has not yet been investigated and remains an important question. The high-purity 13.8-Å diameter SWNT samples that have recently been produced by laser vaporization[30] should be interesting candidates for evaluation. The temperature and pressure requirements for H₂ adsorption and desorption, and the kinetics for charging and discharging, are expected to be a function of nanotube diameter and aspect ratio. Control of these parameters coupled with improvements in production, purification and alignment of SWNTs may lead to a new H₂ storage technology for hydrogen-fuelled vehicles with superior performance to currently available options.

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Spontaneous stratification in granular mixtures

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Granular materials—such as sand—segregate according to grain size when exposed to periodic perturbations such as vibrations[1–5]. Moreover, mixtures of grains of different sizes can also spontaneously segregate in the absence of external perturbations: when such a mixture is simply poured onto a pile, the large grains are more likely to be found near the base, while the small grains are more likely to be near the top[6–10]. Here we report another size-separation effect, which arises when we pour a granular mixture between two vertical plates: the mixture spontaneously stratifies into alternating layers of small and large grains whenever the large grains have larger angle of repose than the small grains. We find only spontaneous segregation, without stratification, when the large grains have smaller angle of repose than the small grains. The stratification is related to the occurrence of avalanches: during each avalanche, the grains separate into a pair of static layers, with the small grains forming a sublayer underneath the layer of large grains.

Our experimental system consists of a vertical ‘quasi-two-dimensional’ cell with a gap of 5 mm separating two transparent plates (made of Plexiglass or glass) measuring 300 mm × 200 mm (Fig. 1a). To avoid the effects of electrostatic interactions between the grains and the wall, the wall is cleaned with an antistatic cleaner.

In a first series of experiments, we closed the left edge of the cell leaving the right edge free, and we poured, near the left edge, an equal-volume mixture of white glass beads (mean size 0.27 mm, spherical shape, repose angle 26°), and red sugar crystals (typical size 0.8 mm, cubic shape, repose angle 39°). Figure 1a shows the result of the first series of experiments. We note two features: (1) Spontaneous stratification. We see the formation of alternating layers consisting of small and large grains—with a ‘wavelength’ of ~1.2 cm. (2) Spontaneous segregation. We find that the smaller grains segregate near the left edge and the larger grains segregate furthest from it and near the base[13–20].

In a second series of experiments, we confirmed the results of these initial experiments by testing for stratification and segregation using mixtures of grains of same density, consisting of fine sand (typical size 0.4 mm) and coarse sand (typical size 1 mm), suggesting that the density of the grains may not play an important role in stratification.

In all the above experiments we used mixtures of two types of grain with different shape, and therefore with different angles of repose. In particular we obtained stratification (plus segregation) when we used larger cuboid grains and smaller spherical grains: the angle of repose of the large species was then larger than the angle of repose of the small species. Otherwise we obtained only segregation and not stratification when the large grains were less faceted than the small grains, that is, the large grains had smaller angle of repose than the small grains.

To confirm this, we performed a series of experiments using mixtures of irregular shaped sand grains (repose angle 35°, mean size 0.3 mm), and spherical glass beads (repose angle 26° smaller than the repose angle of the sand grains). We found that stratification
(plus segregation) occurred for two different experiments using spherical beads of size 0.07 mm and 0.11 mm (so that the larger grains had larger repose angle). In contrast, we obtained only segregation but not stratification for two experiments using spherical beads of size 0.55 mm and 0.77 mm (so that the larger grains had smaller repose angle). In all cases the segregation of grains occurred with the smaller grains being found near the left edge of the cell and the larger grains near the base of the cell. These results suggest that the phenomenon of segregation is always expected when pouring a granular mixture of grains of different sizes, no matter what are the values of the angles of repose of the species. However, the phenomenon of stratification is only expected when the large species have larger angle of repose than the small species.

Additionally, we performed a series of experiments (not shown) in which we found similar stratification by using different mixtures of differing size ratio between large and small grains (1.66, 2.1, 2.25, 3.25 and 6.66), suggesting that the phenomenon occurs for a broad regime of grain size ratios. We found a similar stratification when we doubled the gap between the vertical plates of the cell and simultaneously doubled the flow rate of grains.

We propose a physical mechanism responsible for the observed stratification that is related to the fact that not one but rather a pair of layers is formed in the course of each avalanche. When the flow of grains reaches the base of the pile, we find that the grains develop a profile characterized by a well-defined 'kink', at which the grains are stopped (Fig. 1b); but we find that the small grains stop first, so a pair of layers forms with the small grains underneath the large grains. As more grains are added, the kink appears to move upwards in the direction opposite to the flow of grains. Once the kink reaches the top, the pair of layers is complete and the cycle is then repeated: a new avalanche occurs, the kink develops, and a new pair of layers forms.

The 'wavelength' of a pair of layers $\lambda$ can be determined by the mean value of the downward velocity $v$ of the rolling grains during an avalanche, the upward velocity $v'$ of the kink, and the thickness of the layer of rolling grains $R_g$ during the avalanche. If the volume of grains in an avalanche scales approximately as the volume of grains in a well formed kink, we predict $\lambda \approx R_g (v + v')/v'$, and we confirm this relation experimentally.

To test this physical mechanism by computer simulation we
considered a mixture comprising small grains of width one pixel and of height $H_1$, and large grains, also of width one pixel but of height $H_2 > H_1$. To generate an equal-volume mixture, we randomly ‘dropped’ a small grain with probability $p = H_1/(H_1 + H_2)$, and ‘dropped’ a large grain with probability $1 - p$ (Fig. 2).

In critical phenomena, it is often useful to first develop a ‘mean field’ type model (in which, for example, spin orientation is determined by a macroscopic variable, the net magnetization), before devising models in which spin orientation is determined by the microscopic quantities such as the orientations of the other spins comprising the system. In this spirit, we focus first not on the ‘microscopic’ grain motions, but rather on the ‘macroscopic’ angle of the sand pile, whose value alternates in time between the maximum angle of stability $\theta_m$, which defines the onset of an avalanche, and the angle of repose $\theta_r$, which defines the end of the avalanche. Using this model (described in Fig. 2 legend), we found a morphology that displays both segregation and stratification.

In addition to the simplest ‘mean field’ approach, we developed a model in which we treat the individual grain motion in accordance with microscopic rules that depend not on the macroscopic angle of the sand pile, but rather on the local angles formed between each grain and its neighbors. Specifically, the dynamics of the small and large rolling grains are governed by the critical angles of repose corresponding to the interactions between the rolling grain and the static grains of the sand-pile surface. This model incorporates the experimental fact that grains segregate because large grains roll down more easily on top of small grains than small grains on top of large grains (for rolling large grains on top of a surface of small grains, the surface appears smoother than for rolling small grains on top of a surface of large grains). Thus the model correctly predicts that the small grains form a sublayer beneath the large grains. We find stratification, as in the simplest ‘mean field’ model, and also find that the profile of the sandpile displays a kink at which rolling grains are stopped—just as in the experiment.

Next we tested the above principles by generalizing from two grain sizes to three. The experiment resulted in stratification with three layers, with the finest grains on the bottommost of each triplet of layers and the coarsest grains on the topmost layer (see Fig. 1c where the same experimental setup of Fig. 1a is used to obtain an alternation of three layers of grains of three different sizes: 0.15 mm, 0.4 mm and 0.8 mm; a close-up view of the stratification pattern of Fig. 1c is shown in Fig. 1d). We are now performing experiments using a continuum size distribution, as geological rock formations (which also display stratification) generally occur in the presence of a continuum distribution of grain size.

To provide another test of the proposed physical mechanism, we note that if both grains are spherical, there should be no stratification because the angles of repose of the large and small grains are then the same. We confirmed this expectation experimentally. The case of spherical grains was also studied by Williams, who seems to have seen a hint of the stratification effect. However, its origin in that case appears to have been an artefact, presumably because his grains were in fact of slightly different shapes.

We note that Boutroux and de Gennes have recently made considerable progress in developing a general theoretical framework to treat the case of granular flows of two different grains. Their conclusions are consistent with the experiments presented here.

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Closure of the Central American Isthmus and its effect on deep-water formation in the North Atlantic

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Modern ocean thermohaline-driven circulation influences global climate by transporting heat to high latitudes and by affecting the exchange of CO₂ between ocean and atmosphere. North Atlantic Deep Water (NADW) plays a key role in this circulation, and Quaternary climate cycles have been linked to changes in NADW flow. General circulation model simulations indicate that before closure, some 3–4 million years ago, of the Central American Isthmus—the narrow strip of land linking North and South America—the direct flow of low-salinity water from the Pacific to the Atlantic Ocean would have led to a smaller NADW flow. Sedimentation patterns and nutrient proxies support these model results by indicating an increase in NADW flow around the time of isthmus closure, but these records do not allow changes in different NADW sources to be distinguished, and the overall effect of closure on global ocean circulation is poorly known. Here we present Nd, Pb and Sr isotope records preserved by a hydrogenous ferromanganese crust from the NADW flow-path in the western North Atlantic Ocean. These records indicate that the isotopic signal associated with NADW strengthened around 3–4 million years ago showing that deep water that formed in the Labrador Sea made a gradually increasing contribution to NADW flow. These data, taken together with those from the central Pacific Ocean, indicate an increased NADW flow since isthmus closure, and suggest that the closure established today’s general pattern of ocean circulation.

North Atlantic Deep Water possesses a distinct physical, chemical and isotopic signature (see, for example, refs 4, 13–15). In particular, the sources of NADW impart an extremely unradiogenic Nd isotope composition ($e_{NaD} = -13.5 \pm 0.5$ (ref. 15), where $e_{Nd}$ is the measured $^{143}Nd/^{144}Nd$ ratio relative to the chondrite uniform reservoir $^{17}$; see Fig. 2a legend) which reflects local input through erosion of old continental material, consistent with the age of the surrounding land masses. By comparison, Antarctic Bottom Water (AABW), the other major source of deep water in the present-day Atlantic, has a much more radiogenic Nd isotope composition ($e_{NaD} = -8.6 \pm 0.5^{17}$). These differences in isotopic composition ($\Delta e_{NaD} = 4.9 \pm 1.0$) are much larger than the present-day measurement precision for the $^{143}Nd/^{144}Nd$ ratio ($\pm 0.2$ p.p.m. ($2\sigma = 0.20 \times eNaD$). Therefore, in principle, if an appropriate record can be found, it should be possible to detect the variations in seawater chemistry that would occur as a consequence of changes in deep-water circulation.

Hydrogenous ferromanganese crusts grow by direct accumulation of metal oxides from sea water, and thus potentially preserve a record of the chemistry of the sea water from which they grow. Here we present Nd, Pb and Sr isotope data for an Fe–Mn crust (BM1996.05) from the San Pablo seamount in the western North Atlantic (Table 1) which lies close to the path of the Deep Western Boundary Current (the southern extension of NADW) and, hence, should sample ‘well mixed’ NADW on its passage south. The crust is up to 120 mm thick, shows no phosphatization ($P < 0.4\%$; compare refs 12, 18) and little elemental variation, except for Al which shows a distinct break 58 mm from the outer surface (Fig. 1a). Crust sampling and isotopic analysis follows procedures reported elsewhere, and isotopic data are given in Table 1. $\Delta$Sr ages (Fig. 1b), calculated using Sr isotope stratigraphy, indicate that the crust started to grow some 18 Myr ago, and preserves two distinct growth intervals. The first, from 18.2 ± 0.6 to 16.2 ± 0.6 Myr ago and the second, from around 10.2 ± 1.2 Myr ago to the present day. The marked break at 58 mm corresponds to a hiatus of some 6.0 Myr, and correlates with the shift in Al, relating either to cessation of growth or an interval of crust erosion. Crust precipitation is considered to occur when oxygen-rich deep water is brought into contact with Mn–rich water from the oxygen minimum zone. It is interesting to note that the two phases of crust growth correspond to periods when oxygen-rich NADW is considered to have been actively formed. The outer surface does not yield any useful age information, giving an $^{87}Sr/^{86}Sr$ ratio much more radiogenic than the present-day value for sea water, possibly due to the incorporation of detrital phases, or surface contamination during sampling. However, a $^{230}U/^{238}U$ age of 8 ± 0.3 kyr for the same sample indicates that there was no significant break in growth, or loss of material. The sample contains no detectable secondary phases. The fundamental principles of oxygen isotope stratigraphy, although it is not possible to rule out the possibility of isotopic homogenization after growth. However, the preservation of a major growth hiatus that correlates with the break in Al concentration, taken with the systematic nature of the $\Delta$Sr ages, suggests that there has been no significant perturbation of the elemental record. Thus, the ages can be