ECONOPHYSICS: PAST AND PRESENT

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ABSTRACT

This article provides a brief historical review of the relationship between_economics and physics, beginning with_Adam Smith being influenced by Isaac Newton's ideas up to the present day including the new econophysics discipline and some of the tools applied to the economy. Thus, this work is expected to_motivate new researchers who are interested in this new discipline.

Keywords: econophysics, agents, memory, correlation, complex networks

1. INTRODUCTION

The notion of the economy emerged_with the classic book_*The Wealth of Nations* published in 1776_by_Adam Smith and, ever since, it has undergone_several changes. It has been_influenced by various areas of knowledge and even formed some new disciplines. Specifically, her union with math formed mathematical economics and when combined with statistics gave_birth to econometrics. In this context, some models or physical ideas have always influenced the economy in many ways, prior to the emergence of the field of econophysics.

Despite the connection of these two disciplines having already existed for some time, it took more than twenty years for the econophysics name to emerge. According to Schinkus_[1],_a new discipline has arisen making a contribution to the economy, especially the financial markets. In this paper, we intend to provide a brief discussion of the development of this new discipline from the historical aspects to its future prospects. We hope, therefore, that new researchers become_interested in this_topic.

The organization of this paper is structured as follows: Section 2 and 3 provides a brief historical account_of the theories of physics being applied to economics and some subareas from econophysics, respectively. In section 4 we show some of the perspectives of econophysics and finally section 5 presents_our final considerations.

2. BRIEF HISTORICAL ASPECTS

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With the discovery of the law of gravity by Isaac Newton (1643-1727), a new method of research arose, not only in physics, but in science in general, based on rationalism, experimentalism and with it an attempt to understand the universe through analysis, synthesis and application of the inductive method. Subsequently, Adam Smith (1723-1790), a philosopher regarded as the founder of economics sciences, was_strongly influenced by Newton's ideas. According to Hetherington [2], "Adam Smith's efforts to discover the general laws of economics were directly inspired and shaped by the examples of Newton's success end discovering the natural laws of motion."

Another economist who was influenced by the physical sciences – mainly in relation to the equilibrium of bodies in the constitution of its laws – was_Walras. His law of general equilibrium was based on the work of the mathematician Louis Poinsot (1777-1859), who produced his research on the equilibrium of forces before Walras. According to Paula [3], "there is no way to recognize the decisive influence of Poinsot on Walras and not see the Walras book as an application in the field of economy from 'science de l'équilibre des forces." Other essential concepts in economics were also strongly influenced by physics. According to Carbonne et al. [4]:

Adolphe Quetelet (1796–1874) corroborated the idea that physical laws could govern human behavior and also economics. His contemporary philosopher, Auguste Comte (1798–1857), first envisaged the social physics as a scientific discipline alongside astrophysics, geophysics and chemical physics. It is not by chance that these concepts raised in an intellectual climate permeated by the Newtonian ideas. The basic assumptions of neoclassical economics span a wide range of applications and concepts (utility maximization, market supply and demand, equilibrium) and are still influential.

At the beginning of the twentieth century, Louis Bachelier (1870-1940)⁴ in his doctoral thesis in mathematics (*Theory de La Speculation*, published in 1900), admitted that the prices of financial assets followed a random walk⁵. She was supervised by the great mathematician Henry Poincary. Curiously, Bachelier [7] anticipated the ideas from Einstein [8] in five years on the mathematical formalization of *random walk*. Thereby, Bachelier _founded the modern theory of finance which _gave rise to the efficient markets hypothesis (see [9-11] and the Black-Scholes pricing formula options).

⁴"who was under_estimated by his supervisors, perhaps because the title of his thesis was not attractive to mathematicians. Unfortunately, certain historical research follows this legend. But our study of documents shows that this simplified story is far from being correct" [5].

⁵Regarding random walk, "the best decision is made based on the present and not the past, the best example for random walk is the guy coin game or crown if someone throws a coin twice or a thousand times up the likelihood of having to face in both cases is 50%, that is, they are independent identically as in the first move der face, this does not guarantee that the second will give face again and a thousand plays der face this also does not guarantee that the thousandth first move will give face, making a completely independent event" [6].

Years later, Fischer Black and Myron Scholes_managed to solve the problem of finding pricing formula options that had an application in the stock exchange. It is noteworthy that one of their ideas was to use the heat diffusion equation widely used in physics. Black and Scholes sought to publish their ideas in an article sent in October 1970 to the *Journal of Political Economy* (JPE). Editors promptly rejected the article, claiming that Black and Scholes put too much emphasis on finance while neglecting economics [12]. Another journal, *Review of Economics and Statistics* from_Harvard, was also quick to return it; neither journal bothered to ask an expert to examine it. Finally, the_paper_was accepted in the May-June 1973 edition in JPE, however, only after the intercession of two members from_Chicago University [12].

Therefore, the Black and Scholes equation -became a way to determine the "fair" price paid for an option, which from the behavioral point of view, generated greater confidence in investors at the time, since it did not only depend on fundamental analysis, but had a mathematical formula that could carry out such a calculation. Another hypothesis in economics which_helps_illustrate_the relationship between the economy and the physical is the efficient markets hypothesis, as discussed below.

2.1 EFFICIENT MARKET HYPOTHESIS

The efficient markets hypothesis is, currently, one of the most discussed and studied topics in Economic Sciences [13-15]. Thus, the importance of understanding this hypothesis is fundamental to understanding the behavior of financial series_and, doing so, one can get a sense of how finances work.

This hypothesis originated from the doctoral thesis in mathematics by_Louis Bachelier (1870-1947), *Theorie de la speculation*, under the supervision of the eminent mathematician Henry Poincaré. In it, Bachelier_[7]compared the prices of financial assets to a *random walk*. However, his thesis remained forgotten until_Samuelson_[9] discovered the work of the "forgotten" teacher and became_fascinated because it was an attempt to give a more scientific character to financial markets.

After that, Samuelson_[9]tried to give a more rigorous account of the efficient markets hypothesis. He reformulated the hypothesis of random behavior of prices while supposing that agents are rational. However, only with the help of_Eugene [10] and Fama [11]_was the hypothesis better developed to define "the market's ability to reflect all available information on the price of financial assets" [16]. Thus, the *random walk* model can be defined as:

The *random walk* model is based on two different hypotheses: a) the current price of a savings bond reflects all available information indicating that the price movements over time are a series of random numbers (**serial correlation of errors equal to zero**); and b) price changes obey the same probability distribution [10].

A parallel between the hypothesis of efficient and econophysics markets lies in the fact that the formulator of the Eugene Fama hypothesis was guided in his Doctoral Thesis by Benoit Mandelbroat who_despite being a mathematician, had a strong connection with econophysics, having started at least two discussions that today are essential to_this discipline: the study of long-term memory in financial series and whether the distribution of the financial series returns are in power law format.

2.2 POWER LAWS AND THE EMERGENCE OF THE ECONOPHYSICS EXPRESSION

The power law or Pareto's Law was originally studied by economist Vilfredo Pareto (1848-1923)_who was interested in the distribution of income in Italy in 1906. Instead of asking what would be the umpteenth higher income, he asked how many people would have a higher income than_x. Thereby, Pareto defined its distribution as follows:

 $P[X > x] \sim (m/x)^{-k}$

_(1)

Where *m* represents_the lowest salary and m > 0, k > 0 and $x \ge m$ and *k* is an inequality index._The lower the index, the more unequal the distribution of income is. This expression attests that there are many millionaires and a few modest people.

For the_power law, the relevant information is not how many people have a higher salary than x, but how many_people receive exactly *x*. This is the probability distribution function associated_with_PDF (Probability Density Function), associated with DFC (Density Function Cumulative)given by Pareto.

 $P[X = x] \sim x^{-(k+1)} = x^{-a}$ (2)

Note that the exponent of the power law distribution, a = k + 1, k is the parameter of the Pareto distribution. According to Gleria [17]:

The Pareto law is_a classic power law. Thanks to that, sometimes the Levy distributions_are called_Pareto-Levy. Bouchaud and Mezard examined Pareto's law and observed that, if we consider the number of people in the United States who have 1 billion dollars, we find that four times more people have half a billion dollars and four times higher than that will have a quarter of a billion dollars, and so on.

Mandelbroat showed that the price of cotton for half a century fit a distribution in the power law format. Mandelbroat[18]realized that normal distributions could not explain the high fluctuations in the price of cotton, given_that a distribution using the power law format fits the data better. The discovery by_Mandelbroat was of vital importance for the emergence of econophysics_early on as a large number_of the studies involving econophysics are_finding power laws in financial series and demonstrating its importance for financial markets. Despite having discovered this pattern still in the 1960s, the hypothesis that Mandelbroat proposed_remained unused_for decades until in the 1990s, when Eugene Stanley and Rosario Mantegna found the same pattern in financial series helping to found the field of econophysics.

The econophysics name first emerged with_Stanley et al.[19] at a conference held in 1995 in Kolkata. It is a neologism used for the branch of physics of complex systems that seeks to make a complete survey of the statistical properties of financial

markets, using the huge volume of data now available and working methods of statistical physics [16].

Econophysics, since its foundation, was intrinsically linked to seeking extreme events in financial series using power laws to describe them. However, this type of study was marginalized or little considered by most economists, since the main economic assumptions were built based on the normal distribution and large deviations were almost impossible. However, the results found by econophysics indicate that such events are not so_rare, e.g. the 1987 crisis, where the Dow Jones index fell 22%, or the 2008 crisis.

In the 1990s, a growing number of publications began studying the distribution of financial returns using_physics (in particular see[19,20-22]). This first period was marked,_mainly, by the application of power laws in the distribution of financial returns. Other types of studies were the size of cities [23] and executive compensation [24,25].

From the 2000s, econophysics expanded rapidly and began_to study various phenomena that occur not only in the financial markets, but in the economy in general; their applications range from the use of fractal analysis of the returns distributions to models based on evolutionary agents.

3. SOME SUBAREAS

3.1. AGENT-BASED MODELS

Econophysics has advanced and is no longer limited to testing financial series, thus embarking on other paths._One example is the Agent-Based Model (ABM)which has been used in several areas of the economy._Its main advantages are the use of agents with limited rational adaptive behavior and the possibility of micro and macro interaction._Due to the ABM_possessing these characteristics, a workshop was held in Virginia at the end of June 2010, with the organization of America's National Science Foundations and with the presence of many economists including the Fed (Federal Reserve System), Bank of England and some scientists (including physicists, economists and computer scientists), in which they showed how the ABM can be useful to Macroeconomics [26].

3.1.1 Setting Agents

An agent is an entity that perceives its environment through sensors and acts on the same using the implementers; for example, on human agents, the eyes and ears are sensitive, hands and mouth are executors $[2\underline{7}]$. Furthermore, agents can evolve, adapt, learn and still have cognitive abilities $[2\underline{8}]$.

Regarding the interaction between the agents and the environment, when the <u>environment</u> issue encounters a_stimulus, the first captures it with its sensors, and then responds with an action using their executioner's elements. Based on this,_Russel_and Norvig [29]_proposed that the basic structure of an agent is very simple: it has an internal data structure that will be updated with the arrival of new insights, this structure is used in decision-making procedures, which will generate actions to be executed. Therefore, according_to Stefferson_Lima and Rosario_[27] they have the following characteristics:

1. Agents can operate without direct human control or other agents: they are **self-employed.**

2. Agents can act in partnership with humans and with other agents: they **communicate.**

3. Agents can react to various forms of stimulation of domains: they are **reactive.**

4. Agents can make decisions for themselves to fit the defined goals: they are **proactive.**

ABM_is the creation of a population of agents, with the capacity of perception and action similar to the actual components to be simulated. So they can act as if they own the components of a system, and one_should provide them with behaviors and rules that define the possible actions [29-31]. This is done by modeling behaviors, by analyzing the variables of a system and extracting its main features so that they can be incorporated into the respective individuals. According_to Pykas and Fagiolo_[32],_ABM has the following characteristics:

a) Time: Usually it is a model evolving overtime in discrete steps, *t*=1,2,...

b) Agents (or_actors): The system is populated by a number of agents $I_t = \{1, 2, ..., N_t\}$. In many examples, but not necessarily all, the population size is assumed to be constant over time $(N_t=N)$.

c) Microstates (or_actions):Each agent_ $i \in I_t$ is characterized by a L vector of Microstates (or variable micro) $X_{i,t} = (X^{1}_{i,t}, ..., X^{L}_{i,t})$, these variables are easy to handle, can make them endogenous, modifying the agents' decisions (as a product of the company, number of shares that individuals have etc.).

d) Micro-parameters: Each agent is also characterized by a micro-parameter vector H $\theta_i = (\theta_i^1, ..., \theta_i^h)$, which_are slow variables, that is, they can_not be quantified without a time scale in a dynamic process. Therefore, θ_i typically__contains information about the behavior and characteristics of the agents_*i* (Company productivity factors, elasticity of consumption, etc.).

e) Macro-Parameters: The system can be characterized as a whole instead of being characterized by an independent technological vector M (macro-parameters) $\Theta = (\Theta_1, ..., \Theta_M)$ governing all direct attitudes; again, Θ _these variables are slow and cannot be modified by agents.

f) Structure Interaction: In each agent *t*, the way that information is channeled between agents is governed by a chart (directly and possibly weighted) G_t _containing all links ij_t currently_in place of an *i*_agent for *j* agent. The existence of a link ij_t means that the *i*_agent updates its micro-variables $x_{i,t}$. It is affected by the choice made in the past by *j* agent.

g) Micro-decision rules: Each agent is provided with a set of decision rules $\Re_{i,t} = \{R_{i,t} (\cdot | \cdot), b=1,...,B\}$ mapping the observable variables and the next micro-changing period $x_{i,t}$. An example might be: production function, innovation rules.

h) Aggregate Variables: Clustering (average, sum, etc.) from micro-variables can create a vector $K_{macro-variables} x_t = (x_{1t_1,...,x_{kt}})$ containing all relevant information to analyze in the system. Examples include GDP, aggregate demand, unemployment, etc.

After the definition and characterization of ABM, as already shown, we will show its use in econophysics demonstrating_its importance to the economy.

3.1.2 The Importance of ABM in Economics

One of the first studies involving adaptive agents and economic theory was Holland and Miller's_[33]_*Artificial Adaptive Agents in Economic Theory*_emphasizing the many advantages of applying this new methodology, among which we mention two: the ability to control all system variables and environmental conditions as well as working with adaptive agents. Since that time, this new research agenda has grown considerably and currently the number of publications in economics has been significant in relation to other sciences_[34].

In this context, a famous work involving ABM and financial markets was the Santa Fe Artificial Market [35], in which the authors innovated implementing agents that can modify their strategies overtime or had the ability to learning._In_Lux and Marchesi [36] heterogeneous agents were used to find high frequency returns of extreme events, *clustered* volatility and power laws.

Using the ABM methodology in the options market has also found anomalies in a study by Suzuki *et al.* [37] using *traders* with aversion to loss and using the pricing formula of Black-Scholes options. Therefore, ABM studies in finances have found several stylized facts in financial series and it represents a new look, since these anomalies are now treated as events that can occur, approaching most of the stock exchanges, in which there are crises, extreme events and panics, unlike the world of the Efficient Market Hypothesis [10] or the Black-Scholes equation [<u>38</u>] wherein the financial series approaches a normal curve, with the possibility of almost zero crises.

Furthermore, in the words of Le Baron [39]_financial markets are particularly attractive for applications based on an agent model for several reasons:

• First, the main debates in finance on market efficiency and rationality are still unresolved.

- Second, financial time series contain many stylized facts that are not well understood.
- Third, financial markets provide a wealth of data volume that can be analyzed.

Use of ABM in macroeconomics is very recent, with a higher frequency in the last decade. In this sense, Le Baron [40], Hodgson [41] and Farmer and Foley [42] have stressed the need for agents to understand the micro and macroeconomic phenomena, because they can interact with each other and the environment, and agents are rationally limited. Due to these characteristics, Colander et al. [43] proposed the use of agents in Macroeconomics; in their words:

The advantage of Computational Agent economy (<u>Agent</u> Based Models applied economics), in particular, in macroeconomics is that it removes the treated limitations of the analytical limit of macroeconomics. <u>ABM</u> allows researchers to choose the appropriate way to solve problems, including the types of agents, number of each type of agents and the hierarchy of their arrangements. They also allow the researchers consider the interactions between agents simultaneously with their decision, and_study the dynamics of macro interaction between them.

Thus, Dosi et al. [44] built a model of evolutionary cycles and managed to reproduce some stylized facts in macroeconomics as the most volatile investment rather than consumption. The investment showed a pro-cyclical growth and the model showed a multiplier equal to the Keynesian accelerator.

Because of the possibility that they may be incorporated into agent's variables such as learning, routines and evolution (somewhat restricted in traditional modeling firm theory), such qualities, according Pykas and Fagiolo_[32], can assist in the proposal of Nelson and Winter [45]_to study the firm and Macroeconomics evolution. In this context, Hodgson [46]_goes further and proposes ABM as an alternative model for the study of institutions in the twentieth century, since for him the institutions are a set of individuals who are constantly interacting and evolving and not a set of rational and atomized units.

In this way, the contribution of ABM on macroeconomics and/or firm theory is still difficult to measure because the research is fairly recent. However, ABM_has been a challenging methodology and can greatly assist in_understanding macroeconomic policies.

3.2 LONG TERM MEMORY

One way to characterize the long term memory of a time series is to associate it with a property called persistence. The determination of this property is generally related to_a parameter, named H exponent or Hurst exponent. In the literature there are many methods for determining this exponent, but one of the most used is the classic R/S method. Specifically, R/S is a method with empirical bases. It has provided a solution for the problem of a finite reservoir subjected to a random input stream.

The question is based on determining the volume of a reservoir by knowing its water inflow $\xi(t)$, whereas its output flow is equal to the average $\xi(t)$, so that the tank never runs dry or overflows [47].

Considering a time interval τ , the mean inlet flow will be:

$$\left\langle \xi \right\rangle_{\tau} = \frac{1}{\tau} \sum_{i=1}^{\tau} \xi(\tau) \tag{3}$$

Let X(t) be the cumulative difference between the input flow and its average

$$X(t,\tau) = \sum_{u=1}^{t} \left\{ \xi(u) - \left\langle \xi \right\rangle_{t} \right\}, (1 \le t \le \tau)$$

$$(4)$$

The maximum and minimum from (4) represents the minimum and maximum volume of water that passes through the shell in the period τ . Thus, the total volume of the reservoir, so that it never overflows or runs dry, should be the difference between the maximum and minimum from *X*,

$$R(\tau) = \max X(t,\tau) - \min X(t,\tau)$$

$$(5)$$

Obviously $R(\tau)$ depends on the flow $\xi(t)$, which in turn depends on the period considered τ . Hurst investigated many natural phenomena and realized that R depended on the period τ as a power law,

$$\frac{R}{S} = \left(\frac{\tau}{2}\right)^{H} \tag{6}$$

In (6) *S* is the standard deviation of the inflow, defined by:

$$S = \left(\frac{1}{\tau} \sum_{t=1}^{\tau} \left\{\xi(t) - \left\langle \xi \right\rangle_{\tau}\right\}^2\right)^{\frac{1}{2}},\tag{7}$$

Introduced only for the variable *R/S* is a dimensionless number making it easier to compare with other phenomena [48]. Although initially for_hydrogeological reasons, this method has considerable application in economics. For example,_Cajueiro and Tabak [49] proposed testing the assertion found in the literature that emerging financial markets were becoming more efficient over time and checked whether this was_true or not._The calculation of the Hurst exponent was proposed from the *R/S* method over time using a time window of 4 years of data. These data were the stock exchange rates of some emerging countries and Japan and the United States. It was observed that for the latter two $H \approx 0.5$ that is, this market efficiency was related to the value of this Hurst exponent and that emerging countries including Brazil, the Philippines and Thailand had values this <u>H</u> exponent_great than 0.5 which showed that these three countries were not following the literature by_becoming more efficient over time.

Another application of this method was in Souza et al.[50] where_they_used the Hurst exponent by R/S method to investigate the long-term memory in the transition between the fixed exchange rate regimes and floating exchange rate in Brazil.

Rejichi et al. [51] tested the efficiency of the MENA stock market using a certain Hurst Exponent with the R/S method._Mensi et al. [52]_determined the Hurst exponent using the R/S method to measure the degree of long-range dependence displayed by crude indexes for measuring the degree of long-range dependence exhibited by West Texas Intermediate (WTI) and European Brent.

These and other applications of the classical method R/S are the physical point of view and basically work in autocorrelation time series. The application of these methods to the economy has been growing in the econophysics literature, promising a major evolution of this new area in the future.

This revolution continues when we look at another aspect of time series in econophysics associated with cross-correlations, which is one way to observe the behavior of grip a time series with another. As we are working with econophysics these series include the financial market such as: the foreign exchange market with the benchmark interest rate, country risk with international reserves, etc.

3.3 CROSS-CORRELATION

The study of cross-correlation is based on statistics that relates one time series with another. In the literature, a range of theories comprise this analysis. In this article we will focus on the theory [53] measuring the cross-correlation between time series, based on the autocorrelation of them [54] and the study of cross-correlation between time series by power law [55]. In order to improve the understanding of this theory we explore this in more detail below.

The theory of Peng et al. [54] is focused on determining the cross-correlation coefficient without trend, ρ_{DCCA} _coefficient,_which succinctly forms the 5 steps of his determination._Step I. Considering two time series, $\{x_t\}$ and $\{y_t\}$, with t = 1, 2, ..., N, (N is the total number of elements of the time series). Then we integrate time series obtaining_two new series:

$$xx_k = \sum_{t=1}^k x_t$$
 and $yy_k = \sum_{t=1}^k y_t$, $k = 1, 2, ..., N$. (8)

Step II: We have divided these two integrated time series, $\{xx_k\}$ and $\{yy_k\}$, in (N-s) overlapping boxes of equal length s, with $4 \le s \le N/4$.

Step III: We calculate the local trend of each box by the least-squares fit of each series, $xP_i(k)$ and $yP_i(k)$. Now we calculate the covariance of waste in each box by:

$$f_{xy}^{2}(s,i) = \frac{1}{s+1} \sum_{k=i}^{i+s} (xx_{k} - xP_{i}(k))(yy_{k} - yP_{i}(k)).$$
(9)

Step IV: Now, the average over all overlapping boxes is calculated for the new covariance function:

$$F^{2}_{xy}(s) = \frac{1}{(N-s)} \sum_{i=1}^{N-s} f^{2}_{xy}(s,i).$$
⁽¹⁰⁾

Step V: Finally we calculate the cross-correlation coefficient ρ_{DCCA} by:

$$\rho_{DCCA}(s) = \frac{F^2_{xy}(s)}{F_{xx}(s)F_{yy}(s)}.$$
(11)

Where $_{xy}(s)$ is the correlation function determined by the method from Podobnik and Stanley [55] and $_{F_{xx}}(s)$ and $_{F_{yy}}(s)$ are the autocorrelation functions determined by the method from Peng et al. [54]. This cross-correlation coefficient depends on the size of each box s_{time_scale} . One advantage of this cross-correlation coefficient is measuring the correlation between two time series with different time scales. The ρ_{DCCA} varies in the range $-1 \le \rho_{DCCA} \le 1$, where 1 means_perfect crosscorrelation, -1 perfect anti cross-correlation and 0 there is no correlation.

In conclusion, the determination of the ρ_{DCCA} coefficient has some applications in econophysics. In M. F. da Silva <u>et al [56]</u> this coefficient was used to measure the correlation between the prices of soybeans and corn in Barreiras/Bahia/Brazil_with the Brazilian foreign exchange market. In Wang et al. [57] the ρ_{DCCA} was used to measure the cross-correlation between the larger coins 44 <u>countries</u> on a global network and in Reboredo et al. [58]_the ρ_{DCCA} coefficient_was used to verify the cross-correlation between the exchange rate and the price of oil in different countries before and after the 2008 economic crisis.

The theory of cross-correlation time series is significantly robust and well applicable in econophysics. There is great potential still to be explored in this area of econophysics and therefore a good opportunity for researchers who want to explore new avenues.

3.4 COMPLEX NETWORKS

Complex networks are nodes (vertices) connected by edges, and they can be exemplified by: transport networks (network of airlines in Brazil, networks of roads), social interactions (knowledge networks, scientific collaboration networks), biological networks (regulatory networks of genes and protein interaction networks) and networks in economics (banking networks and networks of exporting countries), etc.

The study of networks began with the resolution of the Königsberg Problem, city of Prussia, currently Kaliningrad, in Russia. After the statement by Leonhard Euler in 1736 that the problem had no solution, mathematics revolutionized not the answer, but the way it was developed. Euler created basic categories like nodes and edges. Two centuries later, mathematicians Paul Erdös and Alfred Rényi, introduced a new concept that allows the study of these networks: the theory of random graphs. The idea was to combine the theory of graphs with the tools of probability theory. Two other fundamental contributions were: the discovery of the small world effect by_Milgron [59] and Watts and Strogatz [60] and networks free of scale [61].

The structure of a complex network is represented in the same way as a graph by which a set *R*, for networks that do not have weights in the links is defined by $R(v, \varepsilon)$, where $v = \{v_1, v_2, v_3...v_N\}$ are the nodes (or vertices) and $\varepsilon = \{e1, e2, e3, ..., eM\}$ are the edges or connections that connect pairs of nodes, considering the number of elements v and ε , *N* and *M*, respectively. To illustrate this complex structure, a simple schematic representation of a network with three edges and three nodes is shown in Figure 1.

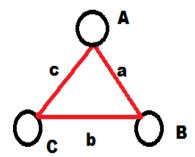


Figure 1: Network consists of three components A, B and C which represent the vertices (nodes) of the network and a, b, c the edges. Source: Self elaboration, 2015.

3.4.1 Complex Network and Financial Markets

The use of complex networks in the financial markets has enabled a new view, mainly to measure the financial interaction between the stock exchanges, assets, banks or companies, in this case, the nodes are usually the assets, banks or countries._For financial markets, the greatest contribution of complex networks to date has been to show the financial markets as interdependent and subject to financial fragility. Until the 2008 crisis, the economy predominated the idea of efficient markets proposal by Eugene [10] where_the assets reflect all available information. However, after the 2008 crisis, markets are not efficient and the financial interconnection between different assets or banks varies greatly (see [62]). This means that in times of financial crisis, stock markets tend to become more interconnected and can completely change the economic and monetary policy of a country.

3.4.2 Complex Networks and Production

Currently, to measure the degree of connection between the various export sectors and importers of the economy, noting that in Hildalgo et al. [63], a new idea about the level of economic growth was formulated. For them an important element is connectivity between some sectors, for example, to produce a computer the company must rely on others that will produce the battery, liquid crystal display, chips, mouse, software, etc. In other words, the more complex and interconnected the relations are between the various sectors, the greater the chances of a country to grow economically, because the greater the knowledge produced by the country in question.

This type of research may represent an advance in the theories of economic growth with an analysis of various disaggregated sectors. Usually, economic models tend to consider only two sectors such as <u>goods</u> and capital. In the case of complex networks there is a paradigm shift in that you can see how each sector interfered in another or the probability of developing a new activity or new sector.

4 PROSPECTS FOR ECONOPHYSICS

The growth of econophysics has been considerable in the last two decades with several indications including the creation of PhD_courses in econophysics around the world such as Houston University or creating econophysics as a discipline in various postgraduate courses both in economics and_in physics. Moreover, many conferences and meetings have_directly and indirectly encompassed econophysics both in Brazil and around the world, with the most well-known being the Econophysics Colloquium, which in 2016 will be_its twelfth year_and has been held in various countries around the world.

Some of the most cited economists in the world, according to various indices that measure the number of citations such as *repec*, *Google Scholar* or *webtometric* use directly or indirectly the theoretical tools of complex systems. For example, Joseph Stiglitz, Nobel laureate in economics, who_has the highest H⁶index of the world according to *webometric* [64] with an H = 177 and one of the most cited according to repec [65], has several works using complex systems and with physical partnerships (see [66-69]). According repec, two of the fifteen most cited economists in the world in the last ten years use complex systems in their recent works Daron Acemoglu and Xavier Gabaix. In the case of Acemoglu, which is the most cited economist in the world in the last ten years, according to repec [65], uses heavy tails to explain the large macroeconomic fluctuations including works with co-author Eugene Stanley, one of econophysics' founders. And the Xavier Gabaix's relationship is even more directly involved with econophysics, as the winner of several awards in economics and finance including the top award Fischer Black of finance, given by the American Finance Association. He uses econophysics in several works mainly using power laws [23,26,70,71] and writing several articles with physicists and with Eugene Stanley.

Another point is the creation of the *Institute for New Economic Thinking*, by mega investor George Soros, with the intention of helping the economic sciences to rebuild and put together strategies to prevent_possible financial crises. The institute has the participation of physicists such as Doyne Farmer from *Santa Fe Institute* and Dirk Helbing from *ETH Zurich (Swiss Federal Institute of Technology in Zurich)*.

In this context, the financial market has been absorbing physicists to work as *traders* or in providing advice, where they can apply the concepts of physics to_complex systems in finance. For that to happen, a great beacon was undoubtedly the 2008 crisis, because while models of physics indicated a likely drop in the North American stock exchange [71], economists were still rooted in the efficient markets hypothesis and that, in addition to physics providing an easier way to deal with complex systems such as the financial markets, it is crucial for greater visibility and application of the concepts or methods of econophysics on stock exchanges [72].

Therefore, economists and physicists are discovering that econophysics can be of great help in modeling various economic problems, leading to a natural process of

⁶ The H-Index_was created in 2005 by the physicist J. E. Hirsch of the University of California. It is a proposal to quantify the productivity and impact of scientists based on papers most cited. In other words, the H index is the number of papers having greater than or equal to this number of quotes. Examples certainly help illustrate the concept: a researcher with H = 5 has 5 papers receiving 5 or more citations; a researcher with H index equal to 30 has published 30 scientific papers, and each received at least 30 citations in other papers_Papers_with fewer_citations would not be considered.

science that is the consolidation of econophysics, just like mathematical economics, behavioral economics and evolutionary_economics.

5 FINAL CONSIDERATIONS

This article explored the contribution physics has had on economics_beginning with Adam Smith being influenced by Newtonian mechanics and the concept of utility or the Black-Scholes formula. Additionally, this paper was shown as a one more discussion's alternative about this topic.

Some instruments used by econophysics were presented such as: power laws, ABM, long term memory, cross-correlation and complex networks in order to provide future researchers in this area information about early concepts in_some of this field's areas. This, of course, does not exhaust all areas of econophysics that, due to its dynamic behavior, also already have good contributions on literature. Therefore, these areas are considered a sample in a universe of possibilities areas to investigate about this topic.

In summary, the emergence of the expression econophysics opened a new horizon of research and scientific contribution that has grown considerably in the last twenty years. Initially, the research was almost exclusively on financial markets, but with a greater number of researchers and the emergence of new techniques, it has expanded and today, there are applications in macroeconomics, theory of the firm, income distribution, microeconomics, etc. This rapid growth of econophysics has brought many perspectives becoming a new discipline, not to be_subsumed by other traditional disciplines within the economy.

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